

Algebra Cheat Sheet

Order of Operations PEMDAS: Properties of Real Numbers:

P=Parenthesis

E= Exponents

M= Multiplication

D= Division

A= Addition

S= Subtraction

Commutative Property: a + b = b + a

Associative Property: (a + b) + c = a + (b + c)

a + -a = 0

Distributive Property: a(b + c) = ab + ac

Zero Property:

a + 0 = aIdentity:

Inverse:

 $a \times 0 = 0$

(ab)c = a(bc)

 $a \times 1 = a$

ab = ba

 $a \times \frac{1}{a} = 1$

Real Numbers:

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... - 2, $-\sqrt{2}$, 0, $\frac{1}{2}$, 1, π , $\sqrt{3}$,...

Rational Numbers:

 $\dots, -\frac{3}{2}, -1, -\frac{1}{2}, 0, \frac{1}{2}, 1, \frac{3}{2}, \dots$

Integers:

 $\dots, -3, -2, -1, 0, 1, 2, 3, \dots$

Whole Numbers:

0,1,2,3,4,5, ...

Natural Numbers:

1,2,3,4,5, ...

Irrational **Numbers:**

.... $-\sqrt{2}$. π . $\sqrt{3}$

Exponent Rules: Combining Like Terms:

 $x^1 \times x^1 = x^{1+1} = x^2$ x + x = 2x

 $\frac{x^1}{x^1} = x^{1-1} = x^0$

3x - x = 2x $3x^2 + x^2 + 5 = 4x^2 + 5$

 $(x^3)^2 = x^{3 \times 2} = x^6$

 $5x^2 - 2x^2 + 10x - 5x = 3x^2 + 5x$

 $(xy)^2 = x^2y^2$

 $10x^2 + 4x - (8x^2 + 2x) =$ $10x^2 + 4x - 8x^2 - 2x = 2x^2 + 2x$ **Factoring Methods to Know:**

Greatest Common Factor (GCF)

Product/Sum

Quadratic Formula: $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

Completing the Square

Difference of Two Squares (DOTS)

Functions and their Equations:

Equation of a Line:

$$y = mx + b$$

$$m = slope$$

$$b = y - intercept$$

Slope Formula:

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{vertical\ change}{horizontal\ change}$$

Quadratic Equation:

$$ax^2 + bx + c = 0$$

Vertex Formula:

$$x = \frac{-b}{2a}$$

Quadratic Equation in vertex form:

$$y = a(x - h)^2 + k$$

Vertex:
$$(h, k)$$

Exponential Equation:

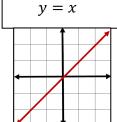
$$y = ab^x$$

Exponential Growth:

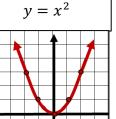
Exponential Decay:

Functions and their Graphs:

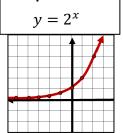
Line



Quadratic



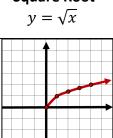
Exponential



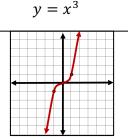
Absolute Value

$$y = |x|$$

Square Root



Cubic Polynomial



Measures of Central Tendency:

Mean: Average

Median: Middle (put numbers in order and find middle)

Mode: "Most" (number that appears the most) **Q1**: Quartile 1=Median of first half of data

Q2: Quartile 2=Median of all data

Q3: Quartile 3=Median of second half of data

Box and Whisker Plot:





Geometric Sequence Formula:

(Use when a sequence is formed by multiplying or dividing a number)

$$a_n = a_1 r^{n-1}$$

 $a_n = Term \ Value$

 $a_1 = First Term$

n = Term Number

r = Common Ratio

Compound Interest Formula:

$$A = P(1 + \frac{r}{n})^{nt}$$

P = Principle

r = Interest rate

 $n = number\ of\ compoundings\ per\ year$

t = Total number of years

Solve for F:
$$C = \frac{5}{9}(F - 32)$$

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$$\frac{5}{9}$$

$$\frac{6}{9}C = F - 32$$

$$\frac{6}{9}C + 32 = F$$

Arithmetic Sequence Formula:

(Use when a sequence is formed by adding or subtracting a number)

$$a_n = a_1 + (n-1)d$$

 $a_n = Term \ Value$

 $a_1 = First Term$

n = Term Number

d = Common Difference

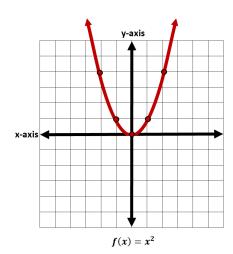
Simplifying Radicals:

$$\sqrt{4}=2$$

$$\sqrt{40} = \sqrt{4 \cdot 10} = \sqrt{4}\sqrt{10} = 2\sqrt{10}$$

$$2\sqrt{18} + \sqrt{32} = 2\sqrt{9 \cdot 2} + \sqrt{16 \cdot 2}$$
$$= 2\sqrt{9}\sqrt{2} + \sqrt{16}\sqrt{2}$$
$$= 2 \cdot 3\sqrt{2} + 4\sqrt{2}$$
$$= 6\sqrt{2} + 4\sqrt{2}$$

Transformations of a Parabola: $f(x) = x^2$:



Function Transformation	What does it do to the graph?	Graph
y = f(x) + C	C > 0 moves up C < 0 moves down	$f(x) = x^2 + 2$
y = f(x + C)	C > 0 moves left C < 0 moves right	$f(x) = (x^2 + 2)$
y = Cf(x)	C > 1 moves closer to $y - axis0 < C < 1$ moves further from $y - axis$	$f(x) = 2x^2$
y = -f(x)	Reflection in the x — axis	$f(x) = -x^2$
y = f(-x)	Reflection in the y — axis	$f(x) = -x^2$

Area and Perimeter:

Shape		Perimeter	Area
Triangle	a c b	P = a + b + c	$A = \frac{1}{2}ab$
Square	s	P = 4s	$A = s^2$
Rectangle	l w	P = 2l + 2w	$A = l \times w$
Trapezoid		P = a + b + 2c	$A = \frac{1}{2}(a+b)h$
Circle	r	$C = \pi d$	$A = \pi r^2$

Tips and Tricks!

Circumference: Cherry Pie's Delicious $C=\pi d$

Area: Apple Pies Are Two $A = \pi r^2$